Let f (from R to R) be Q-linear : additive and f(rx) = r f(x) for all real x and rational r. As we know that a linear function on R is always continuous, can the linearity be relaxed to Q-linearity? Does there exist discontinuous Q-linear function?